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## REPUTATION AND EQUILIBRIUM CHARACTERIZATION IN REPEATED GAMES WITH CONFLICTING INTERESTS

BY KLAUS M. SCHMIDT<sup>1</sup>

A two-person game is of *conflicting interests* if the strategy to which player one would most like to commit herself holds player two down to his minimax payoff. Suppose there is a positive prior probability that player one is a “commitment type” who will always play this strategy. Then player one will get at least her commitment payoff in any Nash equilibrium of the repeated game if her discount factor approaches one. This result is robust against further perturbations of the informational structure and in striking contrast to the message of the Folk Theorem for games with incomplete information.

KEYWORDS: Commitment, Folk Theorem, repeated games, reputation.

### 1. INTRODUCTION

CONSIDER A REPEATED RELATIONSHIP between two long-run players, one of whom has some private information about her type. A common intuition is that the informed player may take advantage of the uncertainty of her opponent and enforce an outcome more favorable to her than that which she would have obtained under complete information. This intuition has been called “reputation effect” and has found considerable attention in the literature. The purpose of this paper is to formalize this intuition in a general model of repeated games with “conflicting interests” and to show that the effect is robust against perturbations of the informational structure of the game.

The first formalization of reputation effects in games with complete information have been developed by Kreps and Wilson (1982) and Milgrom and Roberts (1982). They have shown that a small amount of incomplete information can be sufficient to overcome Selten’s (1978) chain-store paradox. An incumbent monopolist who faces a sequence of potential entrants may deter entry by maintaining a reputation for “toughness” if there is a small prior probability that she is a “tough” type who prefers a price war to acquiescence. Recently, this result has been generalized and considerably strengthened by Fudenberg and Levine (1989, 1992). They consider the class of all repeated games in which a long-run player faces a sequence of short-run opponents, each of whom plays only once but observes all previous play. They show that if there is a positive prior probability of a “commitment type,” who always plays the strategy to which player one would most like to commit herself, and if player

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one is sufficiently patient, then she can enforce at least her commitment payoff in any Nash equilibrium, i.e. she will get at least what she would have obtained if she could have committed herself publicly to this strategy. This result is very powerful, because (i) it gives a tight lower bound for player one's payoff in all Nash equilibria, (ii) it holds for finitely and infinitely repeated games, and (iii) it is robust against further perturbations of the informational structure, i.e. it is independent of what other types may exist with positive probability. However, Fudenberg and Levine's analysis is restricted to games where a long-run player faces a sequence of short-run opponents. Our paper provides a generalization and qualification of their results for the two long-run player case. We show that a necessary and sufficient condition for this generalization to hold is that the game is of conflicting interests.

To make this more precise, consider a repeated game in which player one would like to commit herself to take an action  $a_1^*$ , called her "commitment action," in every period. If player two responds optimally to  $a_1^*$ , player one gets her "commitment payoff." Assume that the game is of "conflicting interests" in the sense that playing  $a_1^*$  holds player two down to his minimax payoff. Now suppose that the informational structure of this game is perturbed such that player one may be one of several possible "types." Consider a type for whom it is a dominant strategy in the repeated game always to play  $a_1^*$  and call her the "commitment type." Our main theorem says that if the commitment type has any arbitrarily small but positive prior probability and if player one's discount factor goes to 1, then her payoff in any Nash equilibrium is bounded below by her commitment payoff. This result is independent of the nature of any other possible types and their respective probabilities. We generalize the theorem to the case of two-sided uncertainty. If the game is not of "conflicting interests" this lower bound does not apply. However, we show that our result may still impose some restriction on the set of equilibrium payoffs.

The main theorem highlights the importance of the relative patience of the two players. Player one has to be sufficiently patient as compared to player two, i.e. for any given discount factor  $\delta_2 < 1$  there exists a  $\underline{\delta}_1(\delta_2) < 1$  such that player one can enforce his commitment payoff in all Nash equilibria if his discount factor satisfies  $\delta_1 > \underline{\delta}_1(\delta_2)$ . The importance of the relative patience of the two players is most intuitive in the case of a completely symmetric game with two-sided uncertainty. If this game has conflicting interests, then it is clearly not possible that both players get their most preferred outcomes at the same time. However, if one of them is sufficiently more patient (or if the prior probability that she is the commitment type is sufficiently higher) then the reputation effect works to her advantage.

In the limit (as  $\delta_1$  approaches 1) our result gives a tight prediction of player one's average payoff in any Nash equilibrium—which seems to be in striking contrast to the message of the Folk Theorem for repeated games with incomplete information. Fudenberg and Maskin (1986) have shown that any feasible payoff vector, which gives each player at least his minimax payoff, can be sustained as an equilibrium outcome if the game is perturbed in the right way.

They assume that with some small probability  $\varepsilon$  each player may be one (and only one) “crazy” type. This crazy type follows a strategy which is tailored to the payoff vector to be sustained as an equilibrium outcome. We follow Fudenberg and Maskin in assuming that one particular type (in our case the “commitment” type) has positive probability. But our approach differs in that we allow for the possibility of arbitrary other types—including the “crazy” types considered by Fudenberg and Maskin. Our result shows that no matter what types may possibly be drawn by nature and how likely they are to occur, if the “commitment type” is present, if player one is sufficiently patient, and if the game has “conflicting interests,” then the commitment type will dominate the play and player one can guarantee herself the commitment payoff in any Nash equilibrium. Thus, in games with conflicting interests the Folk Theorem is not “robust” against further perturbations of the informational structure. If we allow for the possibility of a commitment type of player one, then, as player one’s discount factor approaches 1, all equilibria which give her less than her commitment payoff disappear. We discuss the relation of our results to the Folk Theorem more extensively in Section 4.3.

A complementary analysis to ours is Aumann and Sorin (1989). For a different class of repeated games, coordination games with “common interests,” they obtain a similar result. However, they have to restrict the possible perturbations to types who act like automata with bounded recall. They show that if all strategies of recall zero exist with positive probability, then all pure strategy equilibria will be close to the cooperative outcome. In contrast to Aumann and Sorin we allow for any perturbation of player one’s payoff function and for mixed strategy equilibria. Games of “common” and of “conflicting” interests are two polar cases. We will discuss them in more detail in Section 5.

Finally, in a recent paper Cripps and Thomas (1991) characterize the set of Nash equilibria of infinitely repeated games with one-sided incomplete information in which players maximize the limit of the mean of their undiscounted payoffs. Following a different method pioneered by Hart (1985) they also find that in games of conflicting interests the informed player can enforce her commitment payoff if there is a small prior probability of a commitment type. Since there is no discounting, their result seems to indicate that the relative patience is not that important after all. However, as we will show in Section 4, this interpretation is misleading.

The rest of the paper is organized as follows. In the next section we introduce the model following closely Fudenberg and Levine (1989), and we briefly summarize their main results. Then we give a counterexample showing that their theorem cannot carry over to all repeated games with two long-run players. This gives some intuition on how this class has to be restricted. Section 4 contains our main results. There we generalize Fudenberg and Levine’s (1989) theorem to the two long-run player case, and we show that the restriction to games with “conflicting interests” is a necessary condition for this generalization to hold. Furthermore we extend the analysis to the case of two-sided incomplete information. In Section 5 we give several examples which demon-



strate how restrictive the “conflicting interests” condition is. We also show that even if the game is not of conflicting interests, our results may still be useful to restrict the set of equilibrium outcomes. Section 6 concludes and briefly outlines several extensions of the model.

## 2. DESCRIPTION OF THE GAME

In most of the paper we consider the following very simple model of a repeated game which is an adaptation of Fudenberg and Levine (1989) and Fudenberg, Kreps, and Maskin (1990) to the two long-run player case. The two players are called “one” (she) and “two” (he). In every period they move simultaneously and choose an action  $a_i$  out of their respective action sets  $A_i$ ,  $i \in \{1, 2\}$ . Here we will assume that the  $A_i$  are finite sets.<sup>2</sup> As a point of reference consider the unperturbed game (with complete information) first. Let  $g_i(a_1, a_2)$  denote the payoff function of player  $i$  in the unperturbed stage game  $g$  depending on the actions taken by both players. Let  $\mathcal{A}_i$  denote the set of all mixed strategies  $\alpha_i$  of player  $i$  and (in an abuse of notation)  $g_i(\alpha_1, \alpha_2)$  the expected stage game payoffs.

The  $T$ -fold repetition of the stage game  $g$  is denoted by  $G^T$ , where  $T$  may be finite or infinite. We will deal in most of the paper with the infinite horizon case but all of the results carry over immediately to finitely repeated games if  $T$  is large enough. In the repeated game the overall payoff for player  $i$  from period  $t$  onwards (and including period  $t$ ) is given by

$$(1) \quad V_i^t = \sum_{\tau=t}^{\infty} \delta_i^{\tau-t} g_i^{\tau},$$

where  $\delta_i$  denotes her (his) discount factor ( $0 \leq \delta_i < 1$ ). Our results are stated in terms of average discounted payoffs  $v_i$ , where

$$(2) \quad v_i = (1 - \delta_i) \cdot V_i^1 = (1 - \delta_i) \cdot \sum_{\tau=1}^{\infty} \delta_i^{\tau-1} g_i^{\tau}.$$

After each period both players observe the actions that have been taken. They have perfect recall and can condition their play on the entire past history of the game. Let  $h^t$  be a specific history of the repeated game out of the set  $H^t = (A_1 \times A_2)^t$  of all possible histories up to and including period  $t$ . A pure strategy  $s_i$  for player  $i$  in the repeated game is a sequence of maps  $s_i^t: H^{t-1} \rightarrow A_i$ . Correspondingly, let  $\sigma_i = (\sigma_i^1, \sigma_i^2, \dots)$  denote a mixed (behavioral) strategy of player  $i$ , where  $\sigma_i^t: H^{t-1} \rightarrow \mathcal{A}_i$ . For notational convenience the dependence on history is suppressed if there is no ambiguity. The set of all pure (mixed) strategies is denoted by  $S_i$  ( $\Sigma_i$  respectively).

<sup>2</sup> See Section 6 for the extension to extensive form stage games, continuous strategy spaces, and more than two players.

Let  $B: \mathcal{A}_1 \mapsto \mathcal{A}_2$  be the best response correspondence of player two in the stage game and define<sup>3</sup>

$$(3) \quad a_1^* = \operatorname{argmax}_{a_1 \in A_1} \min_{\alpha_2 \in B(a_1)} g_1(a_1, \alpha_2)$$

as the “commitment action” and

$$(4) \quad g_1^* = \min_{\alpha_2 \in B(a_1)} g_1(a_1^*, \alpha_2)$$

as the “commitment payoff” of player one. That is  $g_1^*$  is the most player one could guarantee for herself in the stage game if she could commit to any pure strategy  $a_1 \in A_1$ . Note that the minimum over all  $\alpha_2 \in B(a_1)$  has to be taken since player two may be indifferent between several best responses to  $a_1$  in which case he may take the response player one prefers least.<sup>4</sup>

Furthermore, let  $\alpha_2^* \in B(a_1^*)$  denote any strategy of player two which is a best response to  $a_1^*$  and define

$$(5) \quad g_2^* = g_2(a_1^*, \alpha_2^*).$$

So  $g_2^*$  is the most player two would get in the stage game if player one were committed to  $a_1^*$ . Suppose  $B(a_1^*) \neq \mathcal{A}_2$  (otherwise the game is “trivial” because player one’s commitment payoff is her maxmin payoff). Then there is an  $\tilde{a}_2 \notin B(a_1^*)$  such that

$$(6) \quad \tilde{g}_2 = g_2(a_1^*, \tilde{a}_2) = \max_{a_2 \notin B(a_1^*)} g_2(a_1^*, a_2) < g_2^*.$$

Note that the maximum exists because it is taken over the finite set of all (pure) actions  $a_2 \notin B(a_1^*)$ . So  $\tilde{g}_2$  is the maximum player two can get if he does not take an action which is a best response against  $a_1^*$ , given that player one takes her commitment action. Finally, define the maximal payoff player two can get at all as

$$(7) \quad \bar{g}_2 = \max_{a_2 \in A_2} \max_{a_1 \in A_1} g_2(a_1, a_2).$$

Clearly, in the repeated game it must be true that

$$(8) \quad V_2' \leq \sum_{\tau=t}^{\infty} \delta_2^{\tau-t} \cdot \bar{g}_2 = \frac{\bar{g}_2}{1 - \delta_2} = \bar{V}_2'$$

for all  $t$  and all  $h^{t-1} \in H^{t-1}$ .

<sup>3</sup> Note that  $a_1^*$  is defined in terms of the stage game. In the repeated game player one may want to commit herself to a more complex strategy which may be nonstationary and dependent on history, e.g. the “tit-for-tat” strategy in the repeated prisoner’s dilemma. All our results hold for history dependent commitment strategies, but nothing is gained by this generalization. Games in which it is strictly desirable to commit to a history dependent strategy do not have conflicting interests as will become clear in Section 5.3. Thus, for notational convenience we restrict attention to stationary commitment strategies. The analysis can also be extended to the more general case where player one would like to commit himself to a mixed strategy. See Fudenberg and Levine (1992) and the remarks in Section 6.

<sup>4</sup> Fudenberg and Levine (1989) refer to  $g_1^*$  as the “Stackelberg payoff.” However, it is now customary to use this expression only for  $\max_{a_1} \max_{\alpha_2 \in B(a_1)} g_1(a_1, \alpha_2)$ , that is for the maximum payoff player one could get if he could publicly commit himself to any action  $a_1$  and player two chooses the best response player one prefers *most*. However, for generic games (in the space of payoff functions) the best reply of player two against  $a_1^*$  is unique. See Fudenberg (1992).

Consider now a perturbation of this complete information game such that in period 0 (before the first stage game is played) the “type” of player one is drawn by nature out of a countable set  $\Omega = (\omega_0, \omega_1, \dots)$  according to the probability measure  $\mu$ . Player one’s payoff function now additionally depends on her type, so  $g_1: A_1 \times A_2 \times \Omega \rightarrow \mathbb{R}$ . The perturbed game  $G^T(\mu)$  is a game with incomplete information in the sense of Harsanyi (1967–68). In the perturbed game a strategy of player one may not only depend on history but also on her type, so  $\sigma_1': H^{t-1} \times \Omega \rightarrow \mathcal{A}_1$ . Two types out of the set  $\Omega$  are of particular importance:

- The “normal” type of player one is denoted by  $\omega_0$ . Her payoff function is the same as in the unperturbed game:

$$(9) \quad g_1(a_1, a_2, \omega_0) = g_1(a_1, a_2).$$

In many applications  $\mu(\omega_0)$  will be close to 1. However, we have to require only that  $\mu(\omega_0) = \mu^0 > 0$ .

- The “commitment” type is denoted by  $\omega^*$ . For her it is a dominant strategy in the repeated game always to play  $a_1^*$ . This is for example the case if her payoff function satisfies

$$(10) \quad g_1(a_1^*, a_2, \omega^*) = g_1(a_1^*, a_2', \omega^*) > g_1(a_1, a_2', \omega^*)$$

for all  $a_1 \neq a_1^*$ ,  $a_1 \in A_1$ , and all  $a_2, a_2' \in A_2$ . The dominant strategy property in the repeated game implies that in any Nash equilibrium player one with type  $\omega^*$  has to play  $a_1^*$  in every period along the equilibrium path. This in turn implies that if  $\mu(\omega^*) = \mu^* > 0$ , then with positive probability there exists a history in any Nash equilibrium with  $s_1^t = a_1^*$  for all  $t$ . The set of all such histories is denoted by  $H^*$ .

We will now restate an important lemma of Fudenberg and Levine (1989) about statistical inference which is basic to the following analysis. The lemma says that if  $\omega^*$  has positive probability and if player two observes  $a_1^*$  being played in every period, then there is a fixed finite upper bound on the number of periods in which player two will believe  $a_1^*$  is “unlikely” to be played. The intuition for this result is the following. Consider any history  $h^{t-1} \in H^*$  in which player one has always played  $a_1^*$  up to period  $t-1$ . Suppose player two believes that the probability of  $a_1^*$  being played in period  $t$  is smaller than  $\bar{\pi}$ ,  $0 \leq \bar{\pi} < 1$ . If player two observes  $a_1^*$  being played in  $t$  he is “surprised” to some extent and will update his beliefs. Because the commitment type chooses  $a_1^*$  with probability 1 while player two expected  $a_1^*$  to be played with a probability bounded away from 1 it follows from Bayes’ Law that the updated probability that he faces the commitment type has to increase by an amount bounded away from 0. However, this cannot happen arbitrarily often because the updated probability of the commitment type cannot become bigger than 1. This gives the upper bound on the number of periods in which player two may expect  $a_1^*$  to be played with a probability less than  $\bar{\pi}$ . Note that this argument is independent of the discount factors of the two players.

To put it more formally: Each (possibly mixed) strategy profile  $(\sigma_1, \sigma_2)$  induces a probability distribution  $\pi$  over  $(A_1 \times A_2)^\infty \times \Omega$ . Given a history  $h^{t-1}$

let  $\pi'(a_1^*)$  be the probability attached by player two to the event that the commitment strategy is being played in period  $t$ , i.e.  $\pi'(a_1^*) = \text{Prob}(s_1' = a_1^* | h^{t-1})$ . Note that since  $h^{t-1}$  is a random variable  $\pi'(a_1^*)$  is a random variable as well. Fix any  $\bar{\pi}$ ,  $0 \leq \bar{\pi} \leq 1$ , and consider any history  $h$  induced by  $(\sigma_1, \sigma_2)$ . Along this history let  $n(\pi'(a_1^*) \leq \bar{\pi})$  be the number (possibly infinite) of the random variables  $\pi'(a_1^*)$  for which  $\pi'(a_1^*) \leq \bar{\pi}$ . Again, since  $h$  is a random variable, so is  $n$ .

LEMMA 1: Let  $0 \leq \bar{\pi} < 1$ . Suppose  $\mu(\omega^*) = \mu^* > 0$ , and that  $(\sigma_1, \sigma_2)$  are such that  $\text{Prob}(h \in H^* | \omega^*) = 1$ . Then

$$(11) \quad \text{Prob} \left[ n(\pi'(a_1^*) \leq \bar{\pi}) > \frac{\log \mu^*}{\log \bar{\pi}} \mid h \in H^* \right] = 0.$$

Furthermore, for any infinite history  $h$  such that the truncated histories  $h_t$  all have positive probability and such that  $a_1^*$  is always played,  $\mu(\omega^* | h_t)$  is nondecreasing in  $t$ .

PROOF: See Fudenberg and Levine (1989), Lemma 1.

One feasible strategy for player one with type  $\omega_0$  is of course to mimic the commitment type and always to play  $a_1^*$ . Lemma 1 does not say that in this case  $\mu(\omega^* | h_t \in H^*)$  converges to 1, i.e. that player two will gradually become convinced that he is facing  $\omega^*$  if he observes  $a_1^*$  always being played. Rather it says that if he observes  $a_1^*$  being played in every period he cannot continue to believe that  $a_1^*$  is “unlikely” to be played.

Suppose that player two is completely myopic, that is he is only interested in his payoff of the current period. Fudenberg and Levine show that there is a  $\bar{\pi} < 1$  such that if the probability that player one will play  $a_1^*$  is bigger than  $\bar{\pi}$ , then a short-run player two will choose a best response against  $a_1^*$ . Thus, if player one mimics the commitment type, then by Lemma 1 her short-run opponents will take  $a_2 \notin B(a_1^*)$  in at most  $k = \log \mu^* / \log \bar{\pi}$  periods. The worst that can happen to player one is that these  $k$  periods occur in the beginning of the game and that in each of these periods she gets

$$(12) \quad \underline{g}_1 = \min_{\alpha_2 \in \mathcal{A}_2} g_1(a_1^*, \alpha_2).$$

This argument provides the intuition for the following theorem.

THEOREM 1 (Fudenberg-Levine): Let  $\delta_2 = 0$ ,  $\mu(\omega^0) > 0$ , and  $\mu(\omega^*) = \mu^* > 0$ . Then there is a constant  $k(\mu^*)$  otherwise independent of  $(\Omega, \mu)$ , such that

$$(13) \quad v_1(\delta_1, \mu^*; \omega^0) \geq (1 - \delta_1^{k(\mu^*)}) \cdot \underline{g}_1 + \delta_1^{k(\mu^*)} \cdot g_1^*,$$

where  $v_1(\delta_1, \mu^*; \omega^0)$  is any average equilibrium payoff to player one with type  $\omega_0$  in any Nash equilibrium of  $G^\infty(\mu)$ .

If  $\delta_1$  goes to 1 the “normal” type of player one can guarantee herself on average at least her commitment payoff no matter what other types may be around with positive probability. The result is discussed in more detail in Fudenberg and Levine (1989). Note however that Theorem 1 is crucially based on the assumption that player two is completely myopic. If he cares about future payoffs, then he may trade off short-run losses against long-run gains. Thus, even if he believes that  $a_1^*$  will be played with a probability arbitrarily close or equal to 1, he may take an action  $a_2$  which is not a short-run best response against  $a_1^*$ . One intuitive reason for this could be that he might invest in screening the different types of player one. Even if this yields losses in the beginning of the game the investment may well pay off in the future. This leads Fudenberg and Levine to conclude that their result does not apply to two long-run player games. The main point of our paper, however, is to show that for a more restricted class of games a similar result holds in the two long-run players case as well. Since player two’s discount factor is smaller than 1, the returns from an investment may not be delayed too far to the future. He will not “test” player one’s type arbitrarily often if the probability that she will play  $a_1^*$  is always arbitrarily close to 1. This idea will be used in Section 4 to prove an analog of Theorem 1 for two long-run player games.

### 3. A GAME NOT OF CONFLICTING INTERESTS

Before establishing our main result let us show that Theorem 1 does not carry over to *all* repeated games with two long-run players. We give a counterexample of a game in which the normal type of player one cannot guarantee herself almost her commitment payoff in all Nash equilibria. The example is instructive for two reasons. First, it shows how to construct an equilibrium in which the normal type of player one gets strictly less than her commitment payoff. This equilibrium is not only a Nash but a sequential equilibrium which survives all standard refinements. Second, the construction leads to a necessary and sufficient condition on the class of games for which Theorem 1 can be generalized to the two long-run player case.

Consider an infinite repetition of the following stage game with three types of player one (see Figure 1). Player one chooses between  $U$  and  $D$  and her payoff is given in the upper left corners of each cell. Clearly the normal type of player

	$L$	$R$		$L$	$R$		$L$	$R$
$U$	10    10	0    0	$U$	10    10	10    0	$U$	1    10	1    0
$D$	0    0	1    1	$D$	0    0	1    1	$D$	1    0	1    1
“normal” type $\mu^0 = 0.8$			“commitment” type $\mu^* = 0.1$			“indifferent” type $\mu^i = 0.1$		

FIGURE 1.—A game with common interests.

one would like to publicly commit always to play  $U$  which would give her a commitment payoff of 10 per period in every Nash equilibrium. For the commitment type it is indeed a dominant strategy in the repeated game always to play  $U$ . The indifferent type, however, is indifferent between  $U$  and  $D$  no matter what player two does.

If  $0.75 \leq \delta_1 \leq 1$  and  $0.95 \leq \delta_2 \leq 1$ , then the following strategies and beliefs form a sequential equilibrium of  $G^\infty$ :

- *Normal type of player one*: “Play  $U$ . If you ever played  $D$ , switch to playing  $D$  forever.”

- *Commitment type of player one*: “Always play  $U$ .”

- *Indifferent type of player one*: “Always play  $U$  along the equilibrium path. If there has been any deviation by any player in the past switch to playing  $D$  forever.”

- *Player two*: “Alternate between 19 times  $L$  and 1 times  $R$  along the equilibrium path. If player one ever played  $D$ , switch to  $R$  forever. If player two himself deviated in the last period, play  $L$  in the following period. If player one reacted to the deviation by playing  $U$ , go on playing  $L$  forever. If she reacted with  $D$ , play  $R$  forever.”

- *Beliefs*: Along the equilibrium path beliefs don’t change. If player two ever observes  $D$  to be played, he puts probability 0 on the commitment type. If player one reacts to a deviation of player two by playing  $U$ , the indifferent type gets probability 0. In both cases the respective two other types may get arbitrary probabilities which add up to 1.

In the limit, as  $\delta_1 \rightarrow 1$ , these strategies give the normal type of player one a payoff of

$$(14) \quad \lim_{\delta_1 \rightarrow 1} v_1(\omega^0) = 9.5 < 10 = g_1^*.$$

Why is this an equilibrium? Consider the normal type of player one. Clearly she would like to signal that she is the normal or the commitment type. Since all three types of player one always play  $U$  along the equilibrium path the only way to transmit information about her type is to play  $D$ . However, playing  $D$  “kills” the commitment type, because for her it is a dominant strategy always to play  $U$ . But without the commitment type it is impossible to get rid of the “bad” equilibrium  $(D, R)$ . What about player two? He expects  $U$  always to be played along the equilibrium path. Nevertheless he plays  $R$ , which is not a short-run best response, in every twentieth period. His problem is that he faces the indifferent type with positive probability. If he chooses  $L$  when he is supposed to play  $R$ , then this might trigger a continuation equilibrium against the indifferent type which gives him far less than that which he would have obtained from playing against the normal or commitment type of player one. It is this risk which sustains the equilibrium outcome.

Note that there are very few restrictions imposed on the updating of beliefs in information sets which are not reached on the equilibrium path. The example only requires that if  $D$  is played for the first time, the commitment type gets

probability 0, which is perfectly reasonable given that for her it is a dominant strategy in the repeated game always to play  $U$ .

To what extent does the example rely on the existence of the indifferent type? Without the indifferent type it is still possible to construct a Nash equilibrium which gives player one less than her commitment payoff. Actually, this is very simple: The normal and the commitment type of player one always play  $U$  along the equilibrium path. After any deviation they switch to playing  $D$  forever. Player two alternates playing one period  $L$  and one period  $R$ . If there has been any deviation, he plays  $R$  forever. If the discount factors are high enough these strategies form a Nash equilibrium for any  $\mu^* > 0$ . Here the average payoff of the normal type of player one is 5. Note, however, that this equilibrium is not sequential. It requires for example that the commitment type plays  $D$  off the equilibrium path.<sup>5</sup>

What sustains both equilibria is the possibility of a continuation equilibrium which punishes player two if he plays his short-run best response against  $a_1^*$  in periods when he is supposed not to do so. Note that this construction does not work if player two is already held down to his minimax payoff by the commitment strategy of player one, since in this case nothing worse can happen to him. In the next section we show that this is the only case in which Fudenberg and Levine's result can be generalized to the two long-run player case.

#### 4. MAIN RESULTS

##### 4.1. *The Theorem*

Suppose that the commitment strategy of player one holds player two down to his minimax payoff. In this case there is no "risk" in playing a best response against  $a_1^*$  because player two cannot get less than his minimax payoff in any continuation equilibrium. This motivates the following definition:

**DEFINITION 1:** A game  $g$  is called a *game of conflicting interests with respect to player one* if the commitment strategy of player one holds player two down to his minimax payoff, i.e. if

$$(15) \quad g_2^* = g_2(a_1^*, \alpha_2^*) = \min_{\alpha_1} \max_{\alpha_2} g_2(\alpha_1, \alpha_2).$$

"Conflicting interests" are a necessary and sufficient condition for our main result. Note that the definition puts no restriction on the possible perturbations of the payoffs of player one. It is a restriction only on the commitment strategy and on the payoff function of player two. We will discuss this class of games extensively and give several examples in Section 5. Clearly, in a game with conflicting interests player two can guarantee himself in any continuation

<sup>5</sup> Whether there exists a *sequential* equilibrium in which player one gets substantially less than 10 if there are only the normal and the commitment type around is an open question. Note, however, that we want to characterize equilibrium outcomes which are robust to general perturbations of the informational structure of the game. From this perspective it makes little sense to restrict attention to two possible types only.

equilibrium after any history  $h_t$  at least

$$(16) \quad \underline{V}_2^{t+1} = \frac{1}{1 - \delta_2} \cdot g_2^*.$$

This is crucial to establish the following result:

LEMMA 2: *Let  $g$  be a game of conflicting interests with respect to player one and let  $\mu(\omega^*) = \mu^* > 0$ . Consider any Nash equilibrium  $(\hat{\sigma}_1, \hat{\sigma}_2)$  and any history  $h'$  consistent with this equilibrium in which player one has always played  $a_1^*$ . Suppose that, given this history, the equilibrium strategy of player two prescribes to take  $s_2^{t+1} \notin B(a_1^*)$  with positive probability in period  $t + 1$ . For any  $\delta_2$ ,  $0 < \delta_2 < 1$ , there exists a finite integer  $M$ ,*

$$(17) \quad M \geq N = \frac{\ln(1 - \delta_2) + \ln(g_2^* - \bar{g}_2) - \ln(\bar{g}_2 - \tilde{g}_2)}{\ln \delta_2} > 0,$$

and a positive number  $\varepsilon$ ,

$$(18) \quad \varepsilon = \frac{(1 - \delta_2)^2 \cdot (g_2^* - \tilde{g}_2)}{\bar{g}_2 - \tilde{g}_2} - \delta_2^M \cdot (1 - \delta_2) > 0,$$

such that in at least one of the periods  $t + 1, t + 2, \dots, t + M$  the probability that player one does not take  $a_1^*$ , given that he always played  $a_1^*$  before, must be at least  $\varepsilon$ .

PROOF: See Appendix.

Let us briefly outline the intuition behind this result. Because  $g$  is of conflicting interests player two can guarantee himself at least  $\underline{V}_2^{t+1} = g_2^*/(1 - \delta_2)$  in any continuation equilibrium after any history  $h_t$ . Therefore, if he tries to test player one's type and takes an action  $s_2^{t+1} \notin B(a_1^*)$  in period  $t + 1$  this must give him an expected payoff of at least  $\underline{V}_2^{t+1}$  for the rest of the game. If player one chooses  $a_1^*$  with a probability arbitrarily close or equal to 1, then choosing an action  $a_2 \notin B(a_1^*)$  yields a "loss" of at least  $g_2^* - \bar{g}_2 > 0$  in this period. Recall that  $\bar{g}_2$  is defined as the maximal payoff player two gets if he does not take a best response against  $a_1^*$ . On the other hand,  $\tilde{g}_2$  is an upper bound on what player two may get in any period in which player one does not take her commitment action, and—of course—he cannot get more than  $g_2^*$  if she plays  $a_1^*$ . But if future payoffs are bounded and  $\delta_2 < 1$ , then the compensation for an expected loss today must not be delayed too far to the future. The numbers  $M$  and  $\varepsilon$  are constructed such that if player two takes a strategy  $s_2^{t+1} \notin B(a_1^*)$  in period  $t + 1$ , then it cannot be true that in each of the next  $M$  periods the probability that player one takes her commitment action is bigger than  $(1 - \varepsilon)$ . Otherwise player two would get less than his minimax payoff in equilibrium, a contradiction. Note that this argument also holds for finitely repeated games if  $T$  is large enough.



Lemma 2 holds in any proper subform of  $G$  as long as player one always played  $a_1^*$  in the history up to that subform. Thus if player two chooses actions  $a_2 \notin B(a_1^*)$  along  $h^*$  in  $n \cdot M$  periods, then in at least  $n$  of these periods the probability that player one does not play  $a_1^*$  must be at least  $\varepsilon$ . Together with Lemma 1 this implies our main theorem:

**THEOREM 2:** *Let  $g$  be of conflicting interests with respect to player one and let  $\mu(\omega^0) > 0$ , and  $\mu(\omega^*) = \mu^* > 0$ . Then there is a constant  $k(\mu^*, \delta_2)$  otherwise independent of  $(\Omega, \mu)$ , such that*

$$(19) \quad v_1(\delta_1, \delta_2, \mu^*; \omega^0) \geq (1 - \delta_1^{k(\mu^*, \delta_2)}) \cdot \underline{g}_1 + \delta_1^{k(\mu^*, \delta_2)} \cdot g_1^*,$$

where  $v_1(\delta_1, \delta_2, \mu^*; \omega^0)$  is any average equilibrium payoff of player one with type  $\omega_0$  in any Nash equilibrium of  $G^x(\mu)$ .

**PROOF:** Consider the strategy for the normal type of player one of always playing  $a_1^*$ . Take the integer  $M = [N] + 1$ , where  $[N]$  is the integer part of  $N$ , and a real number  $\varepsilon > 0$ , where  $N$  and  $\varepsilon$  are defined in Lemma 2. By Lemma 2 we know that if player two takes an action  $a_2 \notin B(a_1^*)$ , then there is at least one period (call it  $\tau_1$ ) among the next  $M$  periods in which the probability that player one will play  $a_1^*$  (denoted by  $\pi_{\tau_1}^*$ ) is smaller than  $(1 - \varepsilon)$ . So

$$(20) \quad \pi_{\tau_1}^* < 1 - \varepsilon \equiv \bar{\pi}.$$

However, by Lemma 1 we know that

$$(21) \quad \pi \left[ n(\pi_i^* \leq \bar{\pi}) > \frac{\ln \mu^*}{\ln \bar{\pi}} \middle| h^* \right] = 0.$$

That is, the probability that player one takes her commitment action cannot be smaller than  $\bar{\pi}$  in more than  $\ln \mu^* / \ln \bar{\pi}$  periods. Therefore, player two cannot choose actions  $a_2 \notin B(a_1^*)$  more often than

$$(22) \quad k = M \cdot \frac{\ln \mu^*}{\ln(1 - \varepsilon)}$$

times. Substituting  $M = [N] + 1$  and  $\varepsilon$  from Lemma 2, we get

$$(23) \quad k(\mu^*, \delta_2) = ([N] + 1) \cdot \frac{\ln \mu^*}{\ln \left( 1 - \frac{(1 - \delta_2) \cdot (g_2^* - \bar{g}_2)}{\bar{g}_2 - \bar{g}_2} + \delta_2^{[N] + 1} \right)}.$$

In the worst case player two chooses these actions in the first  $k(\mu^*, \delta_2)$  periods. This gives the lower bound of the theorem. *Q.E.D.*

If  $\delta_1 \rightarrow 1$  (keeping  $\delta_2$  fixed), then the equilibrium payoff of the normal type of player one is bounded below by her commitment payoff. Thus, in the limit our theorem gives the same lower bound as Fudenberg and Levine's theorem does for the case of a long-run player facing a sequence of short-run opponents.

Their result can be obtained as a special case of Theorem 2 for the class of games with conflicting interests. Note that if  $\delta_2$  goes to 0, then  $N$  goes to 0. So

$$(24) \quad \lim_{\delta_2 \rightarrow 0} k(\mu^*, \delta_2) = \frac{\ln \mu^*}{\ln \left( 1 - \frac{g_2^* - \bar{g}_2}{\bar{g}_2 - \bar{g}_2} \right)} = \frac{\ln \mu^*}{\ln \left( \frac{\bar{g}_2 - g_2^*}{\bar{g}_2 - \bar{g}_2} \right)}.$$

In a game with conflicting interests a short-run player two will play a best response against  $a_1^*$  if

$$(25) \quad g_2^* > \pi \cdot \bar{g}_2 + (1 - \pi) \cdot \bar{g}_2$$

or, equivalently, if

$$(26) \quad \pi > \frac{\bar{g}_2 - g_2^*}{\bar{g}_2 - \bar{g}_2} \equiv \bar{\pi}.$$

Using (26) in Lemma 1 immediately implies Theorem 1.

It is important to note that the lower bound given in Theorem 2 depends on the discount factor of player 2. If  $\delta_2$  increases, so does  $k(\mu^*, \delta_2)$ , and the lower bound is reduced. Hence, to obtain his commitment payoff in equilibrium, player one has to be sufficiently patient as compared to player two. The following corollaries elaborate on the importance of the relative patience of the players.

**COROLLARY 1:** *For any  $\delta_2 < 1$ ,  $\mu^* > 0$  and  $\varepsilon > 0$ , there exists a  $\underline{\delta}_1(\delta_2, \mu^*, \varepsilon) < 1$ , such that for any  $\delta_1 \geq \underline{\delta}_1(\delta_2, \mu^*, \varepsilon)$  the average payoff of the normal type of player one is at least  $g_1^* - \varepsilon$ .*

**PROOF:** Choose  $\underline{\delta}_1$  such that

$$(27) \quad g_1^* - \varepsilon = (1 - \underline{\delta}_1^{k(\mu^*, \delta_2)}) \cdot \underline{g}_1 + \underline{\delta}_1^{k(\mu^*, \delta_2)} \cdot g_1^*.$$

Solving for  $\underline{\delta}_1$  yields

$$(28) \quad \underline{\delta}_1 = \underline{\delta}_1(\mu^*, \delta_2, \varepsilon) = \sqrt[k(\mu^*, \delta_2)]{\frac{g_1^* - \underline{g}_1 - \varepsilon}{g_1^* - \underline{g}_1}} < 1.$$

Clearly, if  $\delta_1 \geq \underline{\delta}_1(\mu^*, \delta_2, \varepsilon)$ , then

$$(29) \quad v_1(\delta_1, \delta_2, \mu^*; \omega^0) \geq (1 - \delta_1^{k(\mu^*, \delta_2)}) \cdot \underline{g}_1 + \delta_1^{k(\mu^*, \delta_2)} \cdot g_1^* \\ \geq (1 - \underline{\delta}_1^{k(\mu^*, \delta_2)}) \cdot \underline{g}_1 + \underline{\delta}_1^{k(\mu^*, \delta_2)} \cdot g_1^* = g_1^* - \varepsilon.$$

*Q.E.D.*

**COROLLARY 2:** *Consider any sequence  $\{\delta_2^n\}$ ,  $\delta_2^n < 1$ ,  $\lim_{n \rightarrow \infty} \delta_2^n = 1$  and fix  $\varepsilon > 0$ . Then there exists a sequence  $\{\delta_1^n\}$ ,  $\delta_1^n < 1$ ,  $\lim_{n \rightarrow \infty} \delta_1^n = 1$ , such that for any  $\{\delta_1^n, \delta_2^n\}$  the average payoff of the normal type of player one is bounded below by  $g_1^* - \varepsilon$ .*

PROOF: Take any  $\{\delta_2^n\}$  and fix  $\varepsilon > 0$ . Choose  $\{\delta_1^n\} \rightarrow 1$  such that  $\delta_1^n > \underline{\delta}_1(\delta_2^n, \mu^*, \varepsilon)$  for all  $n$ , where  $\underline{\delta}_1(\delta_2^n, \mu^*, \varepsilon)$  is given by (28). Then the result follows immediately from the previous corollary. *Q.E.D.*

Corollary 2 shows that there is an area in the  $(\delta_1, \delta_2)$ -space such that for any sequence  $\{\delta_1^n, \delta_2^n\} \rightarrow (1, 1)$  in this area player one gets at least her commitment payoff (up to an arbitrarily small  $\varepsilon$ ) for any pair of discount factors along this sequence. Note, however, that  $\lim_{n \rightarrow \infty} (1 - \delta_1)/(1 - \delta_2) = 0$ , i.e. in the limit player one is infinitely more patient than player two. This observation helps to understand a related result of Cripps and Thomas (1991) who consider repeated games without discounting, in which players maximize the limit of the mean of their payoffs. Under slightly stronger conditions on the possible perturbations they show that if the game has conflicting interests and if there is a positive prior probability of a commitment type, then player one gets at least her commitment payoff as the Banach limit of the mean of her stage game payoffs. However, the case of no discounting obscures the role of the relative patience of the players. We can give examples of equilibria in games with conflicting interests where  $\delta_1 \rightarrow 1$ ,  $\delta_2 \rightarrow 1$ ,  $\lim_{n \rightarrow \infty} (1 - \delta_1)/(1 - \delta_2) > 0$ , and player one's equilibrium payoff is bounded away from her commitment payoff for any  $\{\delta_1^n, \delta_2^n\}$  along this sequence. Thus, if player one is not patient enough as compared to player two, our lower bound does not apply.

If player one has to be much more patient than player two, the reader might be left with the impression that we are essentially back to Fudenberg and Levine (1989) where a long-run player faces a sequence of short-run players. However, this is not the case. First, Fudenberg and Levine's result requires  $\delta_2 = 0$  while here  $\delta_2$  may be arbitrarily close to 1. Second, we are going to show in the next subsection that, whenever the game is not of conflicting interests, it is possible to find an equilibrium which violates Fudenberg and Levine's lower bound no matter how much more patient player one is as compared to player two. Thus, there is a fundamental difference between repeated games in which one player does not care at all about her future payoffs and games in which she does care but is less patient than her opponent. Finally, the importance of the relative patience of the two players is very intuitive as will be shown after we have introduced the case of two-sided uncertainty in subsection 4.3.

#### 4.2. Necessity of the "Conflicting Interests" Condition

The question arises whether Theorem 2 also holds for games which are not of conflicting interests. If the game is not "trivial" in the sense that player one's commitment payoff is equal to her minimax payoff,<sup>6</sup> the answer is no.

PROPOSITION 1: *Let  $g$  be a nontrivial game which is not of conflicting interests. Then for any  $\varepsilon > 0$  there is an  $\eta > 0$  and a  $\underline{\delta}_2 < 1$  such that the following holds:*

<sup>6</sup> It is well known that a player can always guarantee herself at least her minimax payoff in any Nash equilibrium.

*There is a perturbation of  $g$ , in which the commitment type of player 1 has positive probability and the normal type has probability  $(1 - \varepsilon)$ , and there is a sequential equilibrium of this perturbed game, such that the limit of the average payoff of the normal type of player one for  $\delta_1 \rightarrow 1$  is bounded away from her commitment payoff by at least  $\eta$  for any  $\delta_2 > \underline{\delta}_2$ .*

PROOF: See Appendix.

Proposition 1 shows that the condition of conflicting interests is not only sufficient but also necessary for Theorem 2 to hold; in fact, it is a little bit stronger than that in two respects. First, it says that if the game is not of conflicting interests, then it is not only possible to find a Nash equilibrium which violates Fudenberg and Levine's lower bound, but also to find a sequential equilibrium. As has been indicated in Section 3, the construction of a Nash equilibrium using threats which are not credible is much simpler. Secondly, Theorem 2 only requires that  $\mu(\omega^0) > 0$  in the perturbed game. So we could have established necessity by constructing a perturbation which gives a high prior probability to an "indifferent" type who credibly threatens to punish any deviation of player two from the equilibrium path we want to sustain. However, in many economic applications it is natural to assume that  $\mu(\omega^0)$  is close to 1. This is why we provide a stronger proposition which says that even if  $\mu(\omega^0)$  is arbitrarily close to 1 it is possible to construct a sequential equilibrium in which the payoff of the normal type of player one is bounded away from  $g_1^*$ .

Note that in Proposition 1  $\delta_1 \rightarrow 1$ , while  $\delta_2$  is fixed, so player one may be arbitrarily more patient than player two. Thus, Proposition 1 shows that there is an important difference between games with two long run players, one of whom is more patient than the other, and games in which a long-run player faces a sequence of short-run players. In the latter, Fudenberg and Levine's bound holds for all stage games; in the former, it holds only for games with conflicting interests.

#### 4.3. *Two-sided Incomplete Information and Two-sided Conflicting Interests*

If there are two long-run players it is most natural to ask what happens if there is two-sided uncertainty. Our result can be extended to this case in the following way. Suppose the game is perturbed such that there is incomplete information about both the payoff functions of player one and player two. Let  $\omega_i$  denote player  $i$ 's type which is drawn by nature in the beginning of the game out of the countable set  $\Omega_i$  according to the probability measure  $\mu_i$ ,  $i \in \{1, 2\}$ . Let  $\omega_i^0$  and  $\omega_i^*$  represent the normal and the commitment types, respectively. Finally, suppose that the game is of conflicting interests with respect to player  $i$ , i.e. player  $i$ 's commitment strategy holds player  $j$  down to his minimax payoff. Without loss of generality let  $i = 1$ . Now consider the normal type of player two. In the proof of Lemma 2 we did not say why player two might choose an action

which is not a best response against player one's commitment strategy. He might do so because he wants to test player one's type or because he wants to build up a reputation himself. No matter what the reason is, Lemma 2 states that if he takes  $a_2 \notin B(a_1^*)$ , then he must expect that player one chooses  $s'_1 \neq a_1^*$  in one of the following periods with strictly positive probability. This argument holds for the normal type of player two no matter what other possible types of player two exist with positive probability.

A possible strategy of player one still is to play  $a_1^*$  in every period. If she faces the normal type of player two, then by Theorem 2 there are at most  $k(\mu_i^*, \delta_2)$  periods in which player two will not play a best response against  $a_1^*$ . In the worst case for player one this happens in the first  $k$  periods of the game. On the other hand, if she does not face the normal type of player two her expected payoff is at least  $\underline{g}_1$  in every period. This argument establishes a lower bound for the expected payoff of the normal type of player  $i$  which is given in the following theorem.

**THEOREM 3:** *Let  $g$  be of conflicting interests with respect to player  $i$  and let  $\mu_i(\omega_i^0) = \mu_i^0 > 0$  and  $\mu_i(\omega_i^*) = \mu_i^* > 0$ ,  $i \in \{1, 2\}$ . Then there are constants  $k_i(\mu_i^*, \delta_j)$ , otherwise independent of  $(\Omega_i, \Omega_j, \mu_i)$ , such that*

$$(30) \quad v_i(\delta_1, \delta_j, \mu_i^*, \mu_j^0; \omega_i^0) \geq (1 - \mu_j^0 \delta_i^{k_i(\mu_i^*, \delta_j)}) \underline{g}_i + \mu_j^0 \delta_i^{k_i(\mu_i^*, \delta_j)} g_i^*$$

where  $v_i(\delta_1, \delta_2, \mu_i^*, \mu_j^0; \omega_i^0)$  is any average equilibrium payoff of player  $i$  with type  $\omega_i^0$  in any Nash equilibrium of  $G^\infty(\mu)$ .

Thus, if the probability of the normal type of player two is close to 1 and if player one is very patient, then the lower bound for her average payoff is again close to her commitment payoff.

What can be said if  $g$  has two-sided conflicting interests, i.e. if each player would like to commit to a strategy which holds his opponent down to his minimax payoff? Of course, if there are two-sided conflicting interests and if both players are equally patient, it is impossible that each of them gets his most preferred payoff. But suppose that  $\delta_i$  and  $\delta_j$  differ. The bigger player  $j$ 's discount factor, the bigger is  $k_i(\mu_i^*, \delta_j)$ , i.e. the number of periods in which player  $i$  must expect that a strategy other than the best response against her commitment strategy is played, and the lower is her lower bound. On the other hand, if  $\delta_j$  is kept fixed and  $\delta_i$  goes to 1, then this  $k$  periods become less and less important, and in the limit player  $i$  will get his commitment payoff. This is very intuitive. In a symmetric game with conflicting interests reputation building has an effect only if one of the parties is sufficiently more patient than the other.

Theorems 2 and 3 are in striking contrast to the message of the Folk Theorem for games with incomplete information by Fudenberg and Maskin (1986). The Folk Theorem says that for any finitely or infinitely repeated game there exists an  $\varepsilon$  perturbation of this game (in which each of the players has a different payoff function with a small prior probability  $\varepsilon$ ) such that any individually

rational, feasible payoff vector can be sustained as the outcome of a sequential equilibrium of the perturbed game, if the players are sufficiently patient.<sup>7</sup> To sustain any particular payoff vector as an equilibrium outcome the “right” perturbation has to be chosen, that is there must be one particular “crazy” type with probability  $\varepsilon$  who sustains this equilibrium by following a particular strategy. Theorems 2 and 3 show that this result is not robust against further perturbations of the informational structure. If one of the players is patient enough and if her commitment type has positive probability, then—no matter what other types are around with positive probability—Theorems 2 and 3 impose a tight restriction on the set of equilibrium outcomes in any Nash equilibrium.

We have to be very precise here in what is meant by “robustness.” Fudenberg (1992) argues that strict equilibria can be constructed to prove the Folk Theorem. Thus, if the discount factor is kept fixed, the equilibrium is not upset by introducing arbitrary additional types with a very small probability. In this sense the Folk Theorem is robust. However, if we introduce different types (including the commitment type) with a very small probability, keep the perturbation fixed, and then let the discount factor of player one go to 1, then all equilibria which give player one less than his commitment payoff will eventually break down. Thus, if we are interested in the set of equilibria for  $\delta_1 \rightarrow 1$ , the Folk Theorem is not robust against small perturbations of the informational structure.

## 5. EXAMPLES

### 5.1. *The Chain Store Game*

Consider the classical chain store game, introduced by Selten (1978), with two long-run players. In every period the entrant may choose to enter a market ( $I$ ) or to stay out ( $O$ ), while the monopolist has to decide whether to acquiesce ( $A$ ) or to fight ( $F$ ). Assume that the payoffs of the unperturbed stage game are given in Figure 2.

The monopolist would like to commit to fight in every period which would give her a commitment payoff of 3 and which would hold the entrant down to 0. Since 0 is also player two's minimax payoff, the game is—according to our definition—of conflicting interests with respect to the monopolist. Kreps and Wilson (1982) have analyzed finite repetitions of this game with some incomplete information about the monopolist's type. For a particular perturbation of player one's payoff function they have shown that there are sequential equilibria in which the monopolist gets on average almost her commitment payoff if her discount factor is close enough to 1 and if there are enough repetitions. However, Fudenberg and Maskin (1986) demonstrated that any feasible payoff

<sup>7</sup> Fudenberg and Maskin's Folk Theorem for games with incomplete information considers only finitely repeated games without discounting. However, the extension to discounting and an infinite horizon is straightforward.

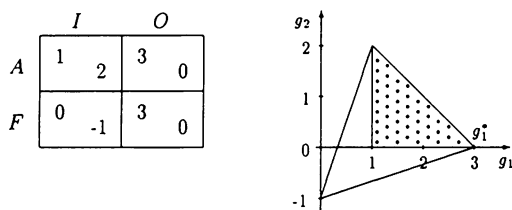


FIGURE 2.—The chain store game.

vector which gives each player more than his minimax payoff, i.e. any point in the shaded area of Figure 2, can be sustained as an equilibrium outcome if the “right” perturbation is chosen. Thus, our Theorem 2 considerably strengthens the result of Kreps and Wilson (1982). It says that the only Nash equilibrium outcome of this game which is robust against any perturbation gives the monopolist at least her commitment payoff of 3 (note that she cannot get more), if she is sufficiently patient as compared to the entrant.<sup>8</sup> Furthermore it shows that this result carries over to the infinitely repeated game.

Now suppose that there is also incomplete information about the payoff function of the entrant. He would like to commit to enter in every period which would give him a commitment payoff of 2 while it would hold the monopolist down to 1, her minimax payoff. So the game is also of conflicting interests with respect to the entrant and our theorem applies. If there is two-sided uncertainty, Proposition 2 says that it all depends on the relative patience of the two players and the prior probability distribution. If player one is sufficiently *more* patient than player two and if the probability of the normal type of player two is close to 1, then player one will get her commitment payoff in any Nash equilibrium, and vice versa.<sup>9</sup>

## 5.2. A Repeated Bargaining Game

Consider a buyer (*b*) and a seller (*s*) who bargain repeatedly in every period on the sale of a perishable good. The valuation of the buyer is 1 and the production costs of the seller are 0. Suppose there is a sealed bid double auction in every period: Both players simultaneously submit bids  $p_b$  and  $p_s$ ,  $p_i \in \{1/n, 2/n, \dots, n/n\}$ , and there is trade at price  $p = (p_b + p_s)/2$  if and only if  $p_b \geq p_s$ . Consider the commitment strategy of the buyer. She would like to commit herself to offer  $p_b^* = 1/n$  in every period. The unique best reply of the

<sup>8</sup> I am grateful to Eric van Damme for the following observation: Theorem 2 does not imply that the average payoff of player two is 0. Recall that player one is more patient than player two. So it may be that in the beginning of the game, say until period  $L$ , she gets less than 3 and player two gets more than 0, but after period  $L$  payoffs are always (3, 0). For player one the first  $L$  periods do not count very much because she is very patient, so her average payoff is 3. However, player two puts more weight on the first  $L$  periods and less on everything thereafter, so her average discounted payoff may be considerably bigger than 0.

<sup>9</sup> Another famous example of a game with conflicting interests is the “Game of Chicken.” See Russell (1959, p. 30) for a description.

seller is  $p_s = 1/n$ , which gives him  $g_s^* = 1/n$ , his minimax payoff. Suppose the payoff function of the buyer is perturbed such that with some positive probability she will always offer  $p_b^*$ . Then Theorem 2 applies and the buyer will get almost her commitment payoff of  $(n-1)/n$  on average in any Nash equilibrium if her discount factor is close to 1.

Note, however, that this example is not as clear-cut as the chain store game. We have to assume that there is a minimal bid  $1/n > 0$ . If the buyer could offer  $p_b = 0$ , she could hold the seller down to a minimax payoff of 0. But if he gets 0, the seller is indifferent between all possible prices, so he might choose  $p_s > 0$  and we end up with no trade. The point is that bargaining over a pie of fixed size is not quite a game of conflicting interests. Some cooperation is needed to ensure that trade takes place at all.

In Schmidt (1992) we consider a more complex extensive form game of repeated bargaining with one-sided asymmetric information, which confirms the above result that the informed player can use the incomplete information about his type to credibly threaten to accept only offers which are very favorable to him. There, however, we take a different approach and it is interesting to compare the two models. In Schmidt (1992) we do not allow for “all possible” but only for “natural” perturbations of player one’s payoff function, i.e. we assume that there may be incomplete information about the seller’s costs,  $c \in [0, 1]$ . We show that, in any sequential equilibrium satisfying a weak Markov property, the buyer will try to test the seller’s type at most a fixed finite number of times, and this will happen only in the end of the game. Surprisingly (from the point of view of Theorem 2) we can show that the seller will get his commitment payoff even if he is much *less patient* than the buyer, so the relative discount factors are not crucial. Furthermore, the bargaining game we consider there is not of conflicting interests.<sup>10</sup> There are common interests as well, because players have to cooperate to some extent in order to ensure that trade takes place.

### 5.3. Games with Common and Conflicting Interests

“Pure” conflicting interests are a polar case and in most economic applications there are both—common and conflicting—interests present. Consider for example the repeated prisoner’s dilemma depicted in Figure 3. In a formal sense this game is of conflicting interests, but our theorem has no bite. Given that player two takes a best response against her commitment action, player one would like most to commit herself to play *D*(effect) in every period. This holds player two down to his minimax payoff, but it only gives player one her minimax payoff as well. So, trivially she will get at least her commitment payoff in every Nash equilibrium. In this game the problem is not to commit to hold player two down to his minimax payoff, but to commit to cooperation.

<sup>10</sup> Note that not all possible perturbations are permitted. This is why conflicting interests are not a necessary condition for the result in Schmidt (1992).



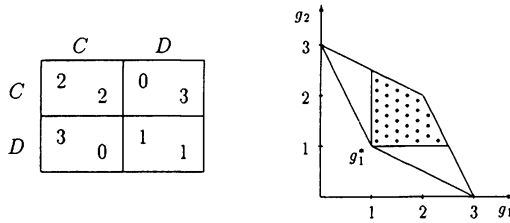


FIGURE 3.—The prisoner's dilemma.

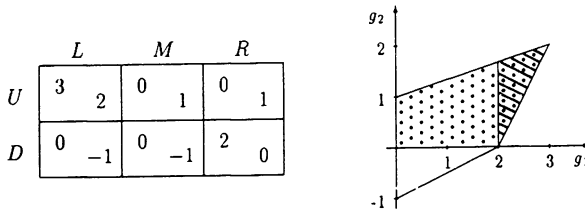


FIGURE 4

In the prisoner's dilemma game player one might do better if she could commit herself to a history dependent strategy such as "tit-for-tat". However, if we allow for the possibility of a "tit-for-tat" commitment type, the game is no longer of conflicting interests: the commitment strategy has to hold player two down to her minimax payoff in every period. For generic games this is only satisfied by stationary commitment strategies.

If the game is not of conflicting interests, Proposition 1 shows that the lower bound of Fudenberg and Levine does not hold. In this case we cannot give a *tight* prediction of player one's equilibrium payoff, but our results may still be useful to restrict the set of equilibrium outcomes as compared to the prediction of the Folk Theorem.<sup>11</sup> To see this, note that our reasoning in Lemma 2 does not rely on the assumption that player one's *most preferred* commitment strategy is to hold player two down to his minimax payoff. If there is positive probability of a type who minimaxes player two, and if the normal type of player one chooses to mimic this type, then there can be only a finite number of periods in which player two does not choose a best response against the minimax strategy. Otherwise he would get less than his minimax payoff. Thus, if player one is patient enough she must get at least as much as she would get if she could publicly commit to the strategy that minimaxes player two.

This is illustrated by the game depicted in Figure 4. Note that the game is not of conflicting interests because the strategy to which player one would most like to commit herself ( $U$ ) does not hold player two down to his minimax payoff. However, player one has the option to mimic a type who always plays  $D$ . This minimaxes player two, so ultimately he has to take a best response against it. Thus, if player one is patient enough she can guarantee herself at least an

<sup>11</sup> I am grateful to Drew Fudenberg for the following observation.

average payoff of 2. In contrast, the Folk Theorem would predict any payoff bigger than 0 for player one.

## 6. EXTENSIONS AND CONCLUSIONS

To keep the argument as clear as possible we considered a very simple class of possible stage games with only two players, finite strategy sets, a countable set of possible types, and commitment types who always take the same pure action in every period. All of these assumptions can be relaxed without changing the qualitative results. Fudenberg and Levine (1989) provide a generalization to  $n$ -player games in which the strategy sets are compact metric spaces and in which there is a continuum of possible types of player one.<sup>12</sup> In Fudenberg and Levine (1992) they show that the argument can be extended to the case where the commitment types play mixed strategies and to games with moral hazard, in which not the action of player one itself but only a noisy signal can be observed by player two. Since the technical problems involved in these generalizations are the same as in our model, we refer to their work for any formal statements and proofs.

Fudenberg and Levine (1989) also demonstrated that the assumption that the stage game is simultaneous-move cannot be relaxed without an important qualification of their Theorem 1. The problem is that in an extensive form game player two may take an action after which player one has no opportunity to show that her strategy is the commitment strategy. Consider for example a repeated bargaining game in which in every period the buyer has to decide first whether to buy or not and then the seller has to choose whether to deliver high or low quality. If the buyer decides not to buy, then he will not observe whether the seller would have produced high quality. This is why the seller might fail to get her commitment payoff in equilibrium. Note however that this problem does not arise in our context. The definition of a game with conflicting interests assumes that the commitment strategy of player one holds player two down to his minimax payoff. Therefore, if player two takes an action  $a_2$  in equilibrium after which player one's commitment strategy  $a_1^*$  is observationally equivalent to some other strategy  $a_1 \neq a_1^*$ , then player two cannot get more than his minimax payoff. So  $a_2$  must have been an element of  $B(a_1^*)$ . However, player one's commitment payoff is defined as  $g_1^* = \max_{a_1 \in A_1} \min_{a_2 \in B(a_1^*)} g_1(a_1, a_2)$ . So if player two chooses  $a_2 \in B(a_1^*)$  player one cannot get less than  $g_1^*$ . Therefore, following Theorem 2 of Fudenberg and Levine (1989), it is straightforward that our result holds without qualification if  $g$  is any finite extensive form game.

To conclude, this paper has shown that "reputation effects" give rise to a tight prediction of the equilibrium outcome in repeated games with conflicting interests. If one of the players is very patient as compared to the other player, then any Nash equilibrium outcome which is robust against perturbations of the

<sup>12</sup> If  $n \geq 3$ , the definition of a game of conflicting interests requires that  $a_1^*$  hold all other players  $i = 2, \dots, n$  down to their minimax payoffs simultaneously.

informational structure gives her on average almost her commitment payoff. This indicates that the message of the Folk Theorem may be misleading. However, we still know very little about the evolution of commitment and cooperation in games in which both—common and conflicting—interests are present, which clearly is one of the most important issues of future research.

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## APPENDIX

PROOF OF LEMMA 2: Consider any equilibrium  $(\sigma_1, \sigma_2)$  and fix a history  $h'$  up to any period  $t$  along which player one has always played  $a_1^*$ , such that  $h'$  has positive probability given  $(\sigma_1, \sigma_2)$ . Such a history exists because  $\mu^* > 0$ . Suppose that according to the (possibly mixed) equilibrium strategy  $\sigma_2^{t+1}$  player two chooses  $s_2^{t+1} \notin B(a_1^*)$  in period  $t+1$  with positive probability. Suppose further that the probability of player one not playing  $a_1^*$  (given that he always played  $a_1^*$  before) in each of the periods  $t+1, t+2, \dots, t+M$  is smaller than  $\varepsilon$ . It will be shown that this can't be true in equilibrium because then player two would get less than his minimax payoff.

Note that  $\varepsilon$  is independent of  $t$  and that  $M$  has been chosen in a way to guarantee that  $\varepsilon > 0$ . Define  $\pi^\tau(a_1) = \text{Prob}(s_1^\tau = a_1 | h^{\tau-1})$  and let  $V_2^\tau(s_1^\tau, \sigma_2^\tau)$  be the continuation payoff of player two from period  $\tau$  onwards (and including period  $\tau$ ) given the strategy profile  $(s_1^\tau, \sigma_2^\tau)$  in period  $\tau$ . The expected payoff of player two from period  $t+1$  onwards is given by

$$\begin{aligned}
 (31) \quad & V_2^{t+1}(\sigma_1, \sigma_2) \\
 &= \sum_{a_1 \neq a_1^*} \pi^{t+1}(a_1) \cdot V_2^{t+1}(a_1, s_2^{t+1}) + \pi^{t+1}(a_1^*) \\
 &\quad \cdot \left\{ g_2(a_1^*, s_2^{t+1}) \right. \\
 &\quad + \delta_2 \cdot \sum_{a_1 \neq a_1^*} \pi^{t+2}(a_1) \cdot V_2^{t+2}(a_1, \sigma_2^{t+2}) + \delta_2 \cdot \pi^{t+2}(a_1^*) \\
 &\quad \cdot \left\{ g_2(a_1^*, \sigma_2^{t+2}) \right. \\
 &\quad + \dots + \\
 &\quad + \delta_2 \cdot \sum_{a_1 \neq a_1^*} \pi^{t+M}(a_1) \cdot V_2^{t+M}(a_1, \sigma_2^{t+M}) \\
 &\quad \left. \left. + \delta_2 \cdot \pi^{t+M}(a_1^*) \cdot \left\{ g_2(a_1^*, \sigma_2^{t+M}) + \delta_2 \cdot V_2^{t+M+1} \right\} \dots \right\} \right\}.
 \end{aligned}$$

It will be convenient to subtract  $\bar{g}_2$  from both sides of the equation in every period. (Recall that  $\bar{g}_2$  is the maximal payoff for player two if he takes an action which is not a best response against  $a_1^*$ .)

Then we get

$$\begin{aligned}
 (32) \quad V_2^{t+1}(\sigma_1, \sigma_2) - \frac{\bar{g}_2}{1 - \delta_2} \\
 = \sum_{a_1 \neq a_1^*} \pi^{t+1}(a_1) \cdot \left[ V_2^{t+1}(a_1, s_2^{t+1}) - \frac{\bar{g}_2}{1 - \delta_2} \right] \\
 + \pi^{t+1}(a_1^*) \cdot \left\{ \left[ g_2(a_1^*, s_2^{t+1}) - \bar{g}_2 \right] \right. \\
 + \delta_2 \sum_{a_1 \neq a_1^*} \pi^{t+2}(a_1) \cdot \left[ V_2^{t+2}(a_1, \sigma_2^{t+2}) - \frac{\bar{g}_2}{1 - \delta_2} \right] \\
 + \delta_2 \cdot \pi^{t+2}(a_1^*) \cdot \left\{ \left[ g_2(a_1^*, \sigma_2^{t+2}) - \bar{g}_2 \right] \right. \\
 + \cdots + \\
 + \delta_2 \cdot \sum_{a_1 \neq a_1^*} \pi^{t+M}(a_1) \\
 \cdot \left[ V_2^{t+M}(a_1, \sigma_2^{t+M}) - \frac{\bar{g}_2}{1 - \delta_2} \right] \\
 + \delta_2 \cdot \pi^{t+M}(a_1^*) \cdot \left\{ \left[ g_2(a_1^*, \sigma_2^{t+M}) - \bar{g}_2 \right] \right. \\
 \left. \left. + \delta_2 \cdot \left[ V_2^{t+M+1} - \frac{\bar{g}_2}{1 - \delta_2} \right] \right\} \cdots \right\}.
 \end{aligned}$$

By assumption the conditional probability that player one does not take her commitment action given that she always played  $a_1^*$  before is smaller than  $\varepsilon$  in any period from  $t + 1, \dots, t + M$ , so

$$(33) \quad \sum_{a_1 \neq a_1^*} \pi^{t+i}(a_1) < \varepsilon,$$

and, of course, we can use that  $\pi^{t+i}(a_1^*) \leq 1$ . Since  $\bar{g}_2$  is the maximal payoff player two can get at all, it has to be true that

$$(34) \quad V_2^{t+i}(a_1, \sigma_2^{t+i}) \leq \frac{\bar{g}_2}{1 - \delta_2} \quad \text{and} \quad V_2^{t+M+1} \leq \frac{\bar{g}_2}{1 - \delta_2}.$$

Furthermore,  $s_2^{t+1}$  is supposed not to be a best response against  $a_1^*$ , so

$$(35) \quad g_2(a_1^*, s_2^{t+1}) \leq \bar{g}_2.$$

Finally we can use that  $g_2(a_1^*, \sigma_2) \leq \bar{g}_2^*$ . Substituting these expressions yields:

$$\begin{aligned}
 (36) \quad V_2'^{+1}(\sigma_1, \sigma_2) - \frac{\bar{g}_2}{1 - \delta_2} &< \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + 1 \\
 &\cdot \left\{ (\bar{g}_2 - \bar{g}_2) + \delta_2 \cdot \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} \right. \\
 &\quad \left. + \delta_2 \cdot 1 \cdot \left\{ (g_2^* - \bar{g}_2) + \cdots + \delta_2 \cdot \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + \delta_2 \cdot 1 \right. \right. \\
 &\quad \left. \left. \cdot \left\{ (g_2^* - \bar{g}_2) + \delta_2 \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} \right\} \cdots \right\} \right\} \\
 &= \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + \delta_2 \cdot \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + \delta_2 \cdot (g_2^* - \bar{g}_2) \\
 &\quad + \cdots + \delta_2^{M-1} \cdot \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + \delta_2^{M-1} \cdot (g_2^* - \bar{g}_2) + \delta_2^M \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} \\
 &= \varepsilon \cdot (1 + \delta_2 + \cdots + \delta_2^{M-1}) \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} + \delta_2^M \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} \\
 &\quad + (1 + \delta_2 + \cdots + \delta_2^{M-1}) \cdot (g_2^* - \bar{g}_2) - (g_2^* - \bar{g}_2) \\
 &< \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{(1 - \delta_2)^2} + \delta_2^M \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} - (g_2^* - \bar{g}_2) + \frac{g_2^* - \bar{g}_2}{1 - \delta_2}.
 \end{aligned}$$

Recall from the statement of Lemma 2 that

$$(37) \quad \varepsilon = \frac{(1 - \delta_2)^2 \cdot (g_2^* - \bar{g}_2)}{\bar{g}_2 - \bar{g}_2} - \delta_2^M \cdot (1 - \delta_2) > 0.$$

It is easy to check that  $\varepsilon$  has been chosen such that

$$(38) \quad \varepsilon \cdot \frac{\bar{g}_2 - \bar{g}_2}{(1 - \delta_2)^2} + \delta_2^M \cdot \frac{\bar{g}_2 - \bar{g}_2}{1 - \delta_2} = g_2^* - \bar{g}_2.$$

Therefore we get

$$(39) \quad V_2'^{+1}(\sigma_2) - \frac{\bar{g}_2}{1 - \delta_2} < \frac{g_2^*}{1 - \delta_2} - \frac{\bar{g}_2}{1 - \delta_2}.$$

However, since  $g_2^*$  is player two's minimax payoff, this is a contradiction to the fact that we are in equilibrium. Q.E.D.

**PROOF OF PROPOSITION 1:** The proof is similar to the construction of the counterexample in Section 3. Perturb the game  $g$  such that there are three types of player one, the normal type, the commitment type, and an indifferent type, whose payoff is the same for any strategy profile, with probabilities  $(1 - \varepsilon)$ ,  $\varepsilon/2$ , and  $\varepsilon/2$ , respectively. Let  $\underline{\delta}_2(\varepsilon) = 2/(2 + \varepsilon) < 1$  and suppose  $\delta_2 > \underline{\delta}_2(\varepsilon)$ . Define

$$(40) \quad n = \frac{\ln \left[ 1 - \frac{2(1 - \delta_2)}{\delta_2 \varepsilon} \right]}{\ln \delta_2}$$

and let  $m = [n] + 2$ , where  $[n]$  is the integer part of  $n$ . Given the restriction on  $\delta_2$  it is straightforward to check that  $n$  is well defined and positive.

Since the commitment payoff of player one is strictly greater than her minimax payoff, there exists an action  $\bar{a}_2$  such that  $\bar{g}_1 = g_1(a_1^*, \bar{a}_2) < g_1^*$  and  $\bar{g}_2 = g_2(a_1^*, \bar{a}_2) < g_2^*$ . Suppose that  $\bar{g}_1 > \minmax g_1$  and  $\bar{g}_2 > \minmax g_2$ .<sup>13</sup> We will now construct an equilibrium such that the limit of the average equilibrium payoff of the normal type of player one for  $\delta_1 \rightarrow 1$  is bounded away from her commitment payoff by at least  $\eta$ , where

$$(41) \quad \eta = \frac{1}{m} \cdot [g_1^* - \bar{g}_1] > 0.$$

Suppose

$$1 > \delta_1 \geq \sqrt{\frac{\bar{g}_1 - \bar{g}_1}{\bar{g}_1 - \bar{g}_1 + g_1^* - \bar{g}_1}},$$

where  $\bar{g}_1$  is the maximum payoff player one can get at all. Along the equilibrium path all types of player one play  $a_1^*$  in every period, while player two plays  $a_2^* \in B(a_1^*)$  in the first  $m - 1$  periods, then he plays  $\bar{a}_2$  in period  $m$ , then starts again playing  $a_1^*$  for the next  $m - 1$  periods, and so on. If player one ever deviates from this equilibrium path, player two believes that he faces the normal type with probability 1. In this case we are essentially back in a game with complete information where the Folk Theorem tells us that any individually rational, feasible payoff vector can be sustained as a subgame perfect equilibrium. So without writing down the strategies explicitly we can construct a continuation equilibrium, such that the continuation payoff is  $((1/(1 - \delta_1))\bar{g}_1, (1/(1 - \delta_2))\bar{g}_2)$ . Clearly, the commitment and the indifferent type of player one have no incentive to deviate since  $a_1^*$  is at least weakly dominant for both of them. It is easy to check that—given  $m \geq 2$  and the restriction on  $\delta_1$ —the normal type of player one will not deviate either.

Now suppose player two ever deviates in any period  $t$ . In this case the normal and the commitment type are supposed to play  $a_1^*$  in period  $t + 1$ , while the indifferent type switches to another strategy  $\tilde{a}_1^{t+1} \neq a_1^*$ . If player two does not observe  $a_1^*$  being played in period  $t + 1$ , he puts probability one on the indifferent type. Using the Folk Theorem we can construct a continuation equilibrium in this subform which gives player two  $(1/(1 - \delta_2))\bar{g}_2$  and which would give the normal type of player one  $(1/(1 - \delta_1))\bar{g}_1$ . If, however, player two observes  $a_1^*$  being played in period  $t + 1$  he puts probability 0 on the indifferent type. In the continuation equilibrium of this subform  $(a_1^*, a_2^*)$  are always played along the equilibrium path. If there is any deviation by player one, player two believes that he faces the normal type with probability one and—using the Folk Theorem again—the continuation payoff is  $((1/(1 - \delta_1))\bar{g}_1, (1/(1 - \delta_2))\bar{g}_2)$ . Clearly, always to play  $a_2^*$  is a best response of player two against always  $a_1^*$  and always  $a_1^*$  is a best response for the commitment type against any strategy. It is easy to check that it is also a best response for the normal type of player one, given the “punishment” after any deviation.

We have already shown that the strategies of the players form an equilibrium after any deviation from the equilibrium path and that, given the continuation equilibria, player one has no incentive to deviate from this path. We still have to check that player two’s strategy is a best response along the equilibrium path. The best point in time for a deviation is when player two is supposed to play  $\bar{a}_2$ . If it does not pay to deviate in this period, it never will. Suppose player two does not deviate. Then his payoff is given by

$$(42) \quad \begin{aligned} V_2(\bar{a}_2) &= \bar{g}_2 + \sum_{t=1}^{m-1} \delta_2^t g_2^* + \delta_2^m \bar{g}_2 + \sum_{t=m+1}^{2m-1} \delta_2^t g_2^* + \dots \\ &= \bar{g}_2 + \frac{\delta_2}{1 - \delta_2} \cdot g_2^* - \frac{\delta_2^m}{1 - \delta_2^m} \cdot (g_2^* - \bar{g}_2). \end{aligned}$$

However, if he deviates, the best he can do is to play  $a_2^*$  in period  $t$ . In this case his payoff is given

<sup>13</sup> If for any of the players  $\bar{g}_i \leq \minmax g_i$  the construction of the “punishment equilibria” which are used below to deter any deviation from the equilibrium path is slightly more complex. In this case players have to alternate between the outcomes  $g^*$  and  $\bar{g}$  such that both get on average at least their minimax payoffs.

by

$$(43) \quad V_2(a_2^*) = g_2^* + \delta_2 \cdot \left\{ \left(1 - \frac{\varepsilon}{2}\right) \cdot \frac{1}{1 - \delta_2} \cdot g_2^* + \frac{\varepsilon}{2} \cdot \frac{1}{1 - \delta_2} \cdot \bar{g}_2 \right\}.$$

It is now easy to check that  $\varepsilon$  and  $\delta(\varepsilon)$  have been constructed such that  $V_2(\bar{a}_2) > V_2(a_2^*)$ . Thus we have established that this is indeed an equilibrium path.

We now have to show that along this equilibrium path the average payoff of the normal type of player one is indeed smaller than  $g_1^* - \eta$  when  $\delta_1 \rightarrow 1$ . The equilibrium payoff of the normal type is given by

$$(44) \quad \begin{aligned} V_1 &= \sum_{t=1}^{m-1} \delta_1^{t-1} g_1^* + \delta_1^{m-1} \bar{g}_1 + \sum_{t=m+1}^{2m-1} \delta_1^{t-1} g_1^* + \dots \\ &= \frac{1}{1 - \delta_1} \cdot g_1^* - \frac{1}{\delta_1} \cdot \frac{\delta_1^m}{1 - \delta_1^m} \cdot [g_1^* - \bar{g}_1]. \end{aligned}$$

Therefore the difference between her commitment payoff and her average payoff in this equilibrium is

$$(45) \quad \begin{aligned} g_1^* - (1 - \delta_1) \cdot V_1 &= g_1^* - g_1^* + \frac{1 - \delta_1}{\delta_1} \cdot \frac{\delta_1^m}{1 - \delta_1^m} \cdot [g_1^* - \bar{g}_1] \\ &= \frac{(1 - \delta_1) \cdot \delta_1^{m-1}}{1 - \delta_1^m} \cdot [g_1^* - \bar{g}_1] \\ &= \frac{(1 - \delta_1) \cdot \delta_1^{m-1}}{(1 - \delta_1) \cdot \frac{1 - \delta_1^m}{1 - \delta_1}} \cdot [g_1^* - \bar{g}_1] \\ &= \frac{\delta_1^{m-1}}{\sum_{t=0}^{m-1} \delta_1^t} \cdot [g_1^* - \bar{g}_1] \\ &> \frac{\delta_1^{m-1}}{m} \cdot [g_1^* - \bar{g}_1]. \end{aligned}$$

Taking the limit for  $\delta_1 \rightarrow 1$  we get

$$(46) \quad \lim_{\delta_1 \rightarrow 1} \frac{\delta_1^{m-1}}{m} \cdot [g_1^* - \bar{g}_1] = \frac{1}{m} \cdot [g_1^* - \bar{g}_1] = \eta. \quad Q.E.D.$$

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ANNOUNCEMENTS

ACCEPTED MANUSCRIPTS

THE FOLLOWING MANUSCRIPTS, in addition to those listed in previous issues, have been accepted for publication in forthcoming issues of *Econometrica*.

- DANA, ROSE ANNE: "Existence and Uniqueness of Equilibria When Preferences Are Additively Separable." (Laboratoire de Mathématiques Fondamentales, Université Pierre et Marie Curie, Tour 45-46, 3ème étage, porte 22, 4 Place Jussieu, 75252 Paris, Cedex 05, France.)
- DROST, FEIKE C., AND THEO E. NIJMAN: "Temporal Aggregation of GARCH Processes." (Dept. of Econometrics, Tilburg University, P.O. Box 90153, 5000 LE Tilburg, The Netherlands.)
- ERICKSON, TIMOTHY: "Restricting Regression Slopes in the Errors-in-Variables Model by Bounding the Error Correlation." (U.S. Bureau of Labor Statistics, Div. of Price & Index No. Research, Postal Square Bldg., Room 3105, 2 Massachusetts Ave. NE, Washington, DC 20212-0001.)
- FAFCHAMPS, MARCEL: "Sequential Labor Decisions Under Uncertainty: An Estimable Household Model of West-African Farmers." (Food Research Institute, Stanford University, Stanford, CA 94305-6084.)
- FRAYSSE, JEAN: "Common Agency: Existence of an Equilibrium in the Case of Two Outcomes." (GREMAQ, Université Science Sociales de Toulouse, PL Anatole France, 31042 Toulouse CE, France.)
- STOCK, JAMES H., AND MARK W. WATSON: "A Simple Estimator of Cointegrating Vectors in Higher Order Integrated Systems." (Dept. of Economics, Northwestern University, 2003 Sheridan Rd., Evanston, IL 60208-2600.)



## 1992 ELECTION OF FELLOWS TO THE ECONOMETRIC SOCIETY

THE FELLOWS OF THE ECONOMETRIC SOCIETY elected fifteen new Fellows in 1992. Their names and selected bibliographies are given below.

JESS BENHABIB, Professor of Economics, New York University.

- “The Hopf Bifurcation and the Existence and Stability of Closed Orbits in Multisector Models of Optimal Economic Growth” (with K. Nishimura), *Journal of Economic Theory*, 21(1979), 421–444.
- “Rational Choice and Erratic Behavior” (with R. H. Day), *Review of Economic Studies*, 48(1981), 459–472.
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ANDREW S. CAPLIN, Professor of Economics, Columbia University.

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JACQUES CREMER, Directeur de Recherche au CNRS, GREMAQ, Université des Sciences Sociales.

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GENE M. GROSSMAN, Jacob Viner Professor of International Economics, Woodrow Wilson School, Princeton University.

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